Shadowing-Based Antenna Selection for V2V Communications

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Abstract—Antenna selection (AS) is considered as an ideal approach for improving the performance of vehicle-to-vehicle (V2V) communications, while satisfying the hardware and power limitations that exist in vehicles. However, the promised gain over single antenna schemes is affected by the fast varying wireless channel, since AS is frequently performed using outdated versions of the signal-to-noise ratio. In this paper, we propose an AS scheme that exploits the stationarity of large scale fading. In particular, by adopting shadowing information as an AS criterion, the negative consequences of the outdated channel state information (CSI) can be alleviated, since large-scale fading varies more slowly as compared to small-scale fading. The performance of the proposed technique is analyzed using the criterion of outage probability. It is shown that the new scheme outperforms the corresponding one that is based on outdated CSI, especially in scenarios with mild channel conditions, in terms of fading/shadowing severity. Moreover, empirical results have been used to verify the effectiveness of the considered shadowing model.

I. INTRODUCTION

In V2V communications, due to the continuous motion of the Tx, Rx, and the surrounding scatterers, the channel conditions can change rapidly. Thus, an antenna selection (AS) system that chooses antennas using channel state information (CSI) in practice operates using outdated versions of CSI. As a result, irreducible diversity gain losses are expected, as it has been shown in many studies in the past, e.g., [1], [2]. The performance degradation due to the outdated CSI increases with the speed of vehicle, since higher Doppler shifts arise, which, in limiting scenarios, will result to performance similar to that in single antenna communication systems.

A promising solution to improve this situation is proposed in [3], where a transmit antenna selection (TAS) scheme based on shadowing information (SI) was proposed. In that system, the transmit antenna offering the largest amplitude shadowing variable between the Tx and the Rx is selected. It was shown that as the number of antennas increases, the shadowing consequences on the transmitted signal can be eliminated. The same basic idea was recently adopted in [4], [5] in physical layer security and cooperative relaying scenarios, respectively. For example, in [5], it was also shown that SI-based AS is a promising option for communication systems operating in higher frequencies, e.g., in extremely higher frequency bands. A common observation in all the previously mentioned works is that the exploitation of the SI provides worth-studying opportunities toward designing low complexity communication techniques that offer similar performance with existing CSI-based ones. Here, it should be noted that the shadowing effects, which are induced by obstructing vehicles between Tx and Rx, considerably affect the performance of intervehicular communication systems [6], [7]. However, very few contributions have analytically investigated the impact of large scale fading in these systems and the required countermeasures for improving their performance.

Motivated by the aforesaid observations, in this paper, we propose and analytically investigate a TAS/selection diversity (SD) system that exploits stationarity of large scale fading. The system operates in a composite fading environment, in which small-scale fading and shadowing are modeled using the Rice and the Inverse-Gamma (IG) distributions, respectively. The latter distribution has been recently proposed as an alternative distribution for accurately modeling the shadowing variable variations [8], [9]. Based on this model, mathematically convenient statistical expressions can be derived, in contrast to the cumbersome expressions that are obtained with the lognormal distribution. In this context, important statistical characteristics for the Rice/IG composite model are derived in closed form for a single-input single-output (SISO) communication system. The analysis is then extended to the scenario where multiple antennas exist at both the Tx and the Rx, and the pair that offers the largest amplitude shadowing variable is selected for the communication phase\(^1\). In the derived results, the generic case where independent but non-identically distributed (i.n.d.) fading/shadowing conditions exist is considered. Simplified expressions are also provided for independent and identically distributed (i.i.d.) conditions. Both these scenarios have been studied in order to prepare a reference point. Finally, the empirical data that

\(^1\)Since the shadowing variables vary much more slowly than the received SNR, it is reasonable to assume that their values at the selection and the reception phases are fully (temporally) correlated.
have been also employed verify the appropriateness of
the IG distribution to model shadowing variations.

The remainder of the paper is organized as follows.
In Section II, the system and channel models of the
scheme under consideration are presented. In Section
III, a statistical framework for the received SNR has
been developed. In Section IV, representative numerical
evaluated results and comparisons with measured data
are presented and discussed, while in Section V, the
concluding remarks can be found.

II. SYSTEM AND CHANNEL MODEL

A. System Model

We consider a low complexity communication system
in which both the Tx and the Rx are equipped with one
RF chain and $N_{t}$, $N_{r}$ antennas, respectively. The links
between the Tx and the Rx are simultaneously affected
by both small-and large-scale fading. The received SNR
between the Tx antenna $i$ and Rx antenna $j$ is given by

$$
\gamma_{i,j} = h_{i,j}^2 s_{i,j}^2 \frac{E_s}{N_0} = g_{i,j} p_{i,j},
$$  

(1)

where $h_{i,j}$, $s_{i,j}$ denote the fading and shadowing vari-
ables, respectively, $g_{i,j} = h_{i,j}^2$, $p_{i,j} = s_{i,j}^2 \frac{E_s}{N_0}$, $E_s$
is the average energy per transmitted symbol, and $N_0$ is
the power spectral density of the additive white Gaussian
noise. In traditional CSI-based AS schemes operating in
time-varying mobile communication environments, the
estimated channel condition at the selection phase could
be significantly different from the corresponding one at
the reception instance, due to the fast variations of the
wireless medium. In particular, even in the ideal scenario
where the feedback interval $T_D$ is equal to or less than
channel’s coherence time $T_c$, i.e., the duration within the
channel is approximately constant, a delayed version of
the CSI will be available. An alternative approach is to
select the antenna based on information that depends on
the shadowing conditions [3]. This approach is actually
based on the fact that the decorrelation distance of the
large scale fading is approximately two orders of
magnitude larger than the one of the small-scale fading
[10], for current frequency bands of interest. Therefore,
with SI-based AS, the antennas pair that is selected is the
one providing the maximum averaged received power,
i.e., shadowing variable, over a predetermined time in-
terval. After the antenna-pair selection is performed, the
corresponding index is fed back to the Tx in order to
proceed with the signal transmission. Thus, given that the
$\ell$, $r$th antennas pair is selected, the received SNR

can be expressed as

$$
\gamma_{\ell,r} = g_{\ell,r} \max_{1 \leq i \leq N_{t}, 1 \leq j \leq N_{r}} \{p_{i,j}\} = g_{\ell,r} p_{\text{max}},
$$  

(2)

where $g_{\ell,r}$ depends on the small-scale fading of the
selected pair. It is worth-noting that $g_{\ell,r}$s change in every
channel’s coherence time, whereas $p_{i,j}$s do not.

B. Channel Model

We consider the scenario where line-of-sight (LoS)
conditions co-exist with large-scale variations caused by
shadowing from large objects, e.g., other vehicles [11].
Therefore, Rice and IG distributions have been employed
to model small scale fading and shadowing variations, respectively. The probability density function (PDF) of
$g_{i,j}$ is given by [12, eq. (2.16)]

$$
f_{g_{i,j}}(x) = \frac{(k_{i,j} + 1)}{\Omega} \exp \left( -k_{i,j} - \frac{(k_{i,j} + 1)x}{\Omega} \right) \\
\times I_0 \left( 2\sqrt{\frac{k_{i,j}(k_{i,j} + 1)x}{\Omega}} \right),
$$  

(3)

where $k_{i,j}$ corresponds to the ratio of the power of the
specular component to the average power of the scattered
component, $\Omega = E(g_{i,j})$, with $E(\cdot)$ denoting expec-
tation, and $I_v(\cdot)$ denotes the modified Bessel function of
the first kind and order $v$ [13, eq. (8.406/1)]. Similar to
[8], the shadowing variables $p_{i,j}$ are assumed to follow
IG distribution, with PDF given by

$$
f_{p_{i,j}}(y) = \frac{\pi \alpha_{i,j}^{\alpha_{i,j}+1}}{\Gamma(\alpha_{i,j}) y^{\alpha_{i,j}+1}} \exp \left( -\frac{\pi \alpha_{i,j}}{y} \right),
$$  

(4)

where $\alpha_{i,j} > 1$ is the shaping parameter of the dis-
tribution, related to the severity of the shadowing, $\gamma_{i,j}$
denotes the scaling parameter, related to the average
received SNR, and $\Gamma(\cdot)$ is the gamma function [13, eq.
(8.310/1)]. Using the total probability theorem, the PDF of
the instantaneous received SNR of the $i$, $j$th pair, $\gamma_{i,j}$, is
given by

$$
f_{\gamma_{i,j}}(\gamma) = \int_{0}^{\infty} f_{g_{i,j}}(\gamma/y) f_{p_{i,j}}(y) dy.
$$  

(5)

Substituting (3) and (4) in (5) and using [13, eq.
(6.643/2)], the following expression for the PDF of $\gamma_{i,j}$
is derived

$$
f_{\gamma_{i,j}}(\gamma) = \frac{(k_{i,j} + 1)^{1/2} \exp \left( -k_{i,j} \right) \pi^{\alpha_{i,j}} \alpha_{i,j}}{\sqrt{k_{i,j} \gamma} \left[ (k_{i,j} + 1)^\gamma + \gamma_{i,j} \right]^{\alpha_{i,j}+1/2}}
\times \exp \left[ \frac{k_{i,j}(k_{i,j} + 1)^\gamma}{2((k_{i,j} + 1)^\gamma + \gamma_{i,j})} \right]
\times M_{-\alpha_{i,j} - \frac{1}{2}} \left[ \frac{k_{i,j}(k_{i,j} + 1)\gamma}{(k_{i,j} + 1)^\gamma + \gamma_{i,j}} \right],
$$  

(6)

where $M_{\kappa,\mu}(\cdot)$ denotes the Whittaker function [13, eq.
(9.220/2)]. The corresponding cumulative distribution
function (CDF) expression is given by

$$
F_{\gamma_{i,j}}(\gamma) = \frac{(k_{i,j} + 1)^\gamma \pi^{\alpha_{i,j}} \alpha_{i,j}}{(k_{i,j} + 1)^\gamma + \gamma_{i,j}}
\times \sum_{k_{i,j}=0}^{\alpha_{i,j}-1} \left[ \frac{k_{i,j} \gamma_{i,j}}{(k_{i,j} + 1)^\gamma + \gamma_{i,j}} \right]^{k_{i,j}}
\times L_{k_{i,j}} \left[ -\frac{k_{i,j}(k_{i,j} + 1)^\gamma}{(k_{i,j} + 1)^\gamma + \gamma_{i,j}} \right],
$$  

(7)
with \( L_n(\cdot) \) denoting the Laguerre polynomial [13, eq. (8.970)].

III. TAS/SD STATISTICS

A. Independent and Non-Identically Distributed Conditions

Assuming i.n.d. fading/shadowing conditions, the CDF of \( \gamma_{t,n} \) is given by

\[
F_{\gamma_{t,n}}(\gamma) = 1 - \sum_{i,j=1}^{N_t,N_r} \sum_{x,y \neq i,j}^{\alpha_{x,y}-1} S_{i,j} \frac{\gamma}{B} T(\gamma) \tag{8}
\]

where

\[
T(\gamma) = \left( \frac{h-2}{B \gamma} \right)^{h-2} \exp \left( \frac{1}{B} \frac{B}{(k_{\ell,n} + 1)} \gamma \right) \times \frac{1}{B} \frac{B}{(k_{\ell,n} + 1)} \gamma \times L_t \left( \frac{k_{\ell,n} \gamma (k_{\ell,n} + 1)}{B + (k_{\ell,n} + 1) \gamma} \right) ,
\]

\[
\frac{\gamma}{B} T(\gamma) = \sum_{i,j=1}^{N_t,N_r} \sum_{x,y \neq i,j}^{\alpha_{x,y}-1} S_{i,j} \gamma \frac{\gamma}{B} T(\gamma) \tag{9}
\]

\[
N_t \gamma = \sum_{i,j=1}^{N_t,N_r} \sum_{x,y \neq i,j}^{\alpha_{x,y}-1} S_{i,j} \gamma
\]

B. Independent and Identically Distributed Conditions

For i.i.d. fading/shadowing, i.e., assuming that \( \alpha_{t,j} = \alpha, \gamma_{t,j} = \gamma, k_{t,j} = k \), the CDF expression of \( \gamma_{out} \) is given by

\[
F_{\gamma_{out}}(\gamma) = 1 - \sum_{n_1,n_2,\ldots,n_a=1}^{N_t,N_r} \frac{1}{N_{t,n}^a} \frac{1}{\Gamma(\alpha) N_t^{b-2}} \times \left[ \frac{k N_t \gamma}{N_t \gamma + (k + 1) \gamma} \right]^b \times \left[ \frac{k(k+1) \gamma}{N_t \gamma + (k + 1) \gamma} \right]^{b-1} \tag{13}
\]

The proof of (12), due to space limitation is not presented here.

IV. PERFORMANCE ANALYSIS AND NUMERICAL RESULTS

The performance of the proposed system is investigated using the criterion of OP. The OP is defined as the probability that the output SNR falls below a predetermined threshold \( \gamma_T \) and it can be evaluated as

\[
P_{out} = F_{\gamma_{out}}(\gamma_T), \text{ in which } F_{\gamma_{out}}(\gamma_T) \text{ is given by (11), for the i.n.d. scenario, and by (13), for the i.i.d. scenario.}
A. Numerical Results

First, the appropriateness of the IG distribution to model shadowing effects was studied. To this aim, the empirical data obtained in the channel measurement campaign presented in [15] are employed. These data were collected in an urban pedestrian propagation environment with a stationary Tx and a mobile Rx, resulting in time-varying channel characteristics. In Fig. 1, the empirical PDF of the signal envelope mean (shadow fading) is plotted. In the same figure, for comparison purposes, the corresponding PDFs of Gamma, IG, and lognormal distributions are also plotted, using the method of moments to estimate their parameters. It is shown that all PDFs provide excellent fit to the empirical one. Moreover, in order to more clearly understand which distribution fits better to the measured data, the Kullback-Leibler divergence criterion is used [16]. According to this, the distribution that provides the best fit to the measured data is the one with the minimum value for the distance $d_{KL}$. Our analysis showed that $d_{KL} = 1.8, 1.54, 1.7\%$, for Gamma, IG, and lognormal distributions, respectively. Therefore, it is shown that the IG distribution can be an excellent model for shadow fading in time-varying channel conditions.

In Fig. 2, assuming $k = 4, \alpha = 2, \gamma = 0$dB, the normalized OP is plotted as a function of the outage threshold, $\gamma_T$, for different numbers of Tx and Rx antennas. It is shown that as the number of the antennas increases, the performance improves with a decreased rate. Moreover, a clear performance improvement is achieved with the proposed scheme, as compared to the SISO scenario (with shadowing), where random AS is performed. It is noteworthy that the proposed scheme can be considered as an effective shadowing countermeasure technique, since for scenarios with $N_t, N_r \geq 2$, it provides better performance as compared to a SISO system operating in a non-shadowed environment.

Another important investigation that is also performed concerns the performance comparison between SI- and CSI-based AS schemes, with the latter one employing outdated versions of CSI. In order to do so, the CDF of the output SNR of a CSI-based TAS scheme operating over Rice/IG composite fading environment is required to be evaluated. An exact analytical expression for this CDF has been derived, which due to space limitation, is not presented here. In Fig. 3, assuming $\alpha = 3$, the OP of the proposed scheme and the one that is based on outdated CSI is plotted as a function of the temporal correlation coefficient $\rho_t$, which quantifies the correlation between the exact and the outdated versions of the received SNR. To obtain this figure, the following assumption was made $N_t = 2, N_r = 1$, while three different scenarios regarding the fading/shadowing conditions were considered and presented in the Table included in Fig. 3. It is shown that the performance of the CSI-based system improves as $\rho_t$ increases as well as with an increase of $k$. A general observation is that for reasonable values of the time correlation, i.e., $\rho_t > 0.6$, which corresponds to typical relative velocities, the CSI-based TAS scheme offers better performance in the cases where strong fading effects are present. A reason for this behaviour is that in these scenarios the multipath components are dominant compared to the constant term of the Rice model and thus the technique that offers improved fading countermeasure performance is the one that focuses on the selection of the best fading variable.
i.e., the CSI-based scheme. However, it is noteworthy that the proposed scheme outperforms the one that is based on outdated CSI in all other investigated scenarios, where mild fading conditions and/or lower values of $\rho_t$ exist, which correspond to high velocities. More specifically, for mild fading conditions, i.e., scenarios 2 and 3, the proposed scheme provides better performance for almost the entire region of $\rho_t$. These results reveal that the negative impact of outdated CSI on the system's performance can be alleviated by exploiting the shadowing information. Finally, the Monte Carlo simulations that were included in Figs. 2 and 3 verify the validity of the presented theoretical framework.

V. CONCLUSIONS

The performance of a TAS/SD scheme operating in a V2V communication environment in the presence of composite fading has been analytically investigated. A new AS scheme is proposed in which the antenna selection at both Tx and RX is performed by exploiting the stationarity of the large scale fading. Capitalizing on the slow variations of the shadowing variable, the detrimental consequence of the outdated CSI that is frequently observed in V2V communications is counteracted. The results presented are based on the derived theoretical analysis, simulations, and empirical data. We have shown the appropriateness of the inverse gamma distribution to model the large scale effects as well as the impact of outdated CSI on the system’s performance. Moreover, it was also shown that in practical situations the proposed approach outperforms the one that exploits CSI acquisition, under various fading/shadowing conditions.

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